



Gort!

the day
the Earth
stood
still

SE2832 Introduction to Software Verification

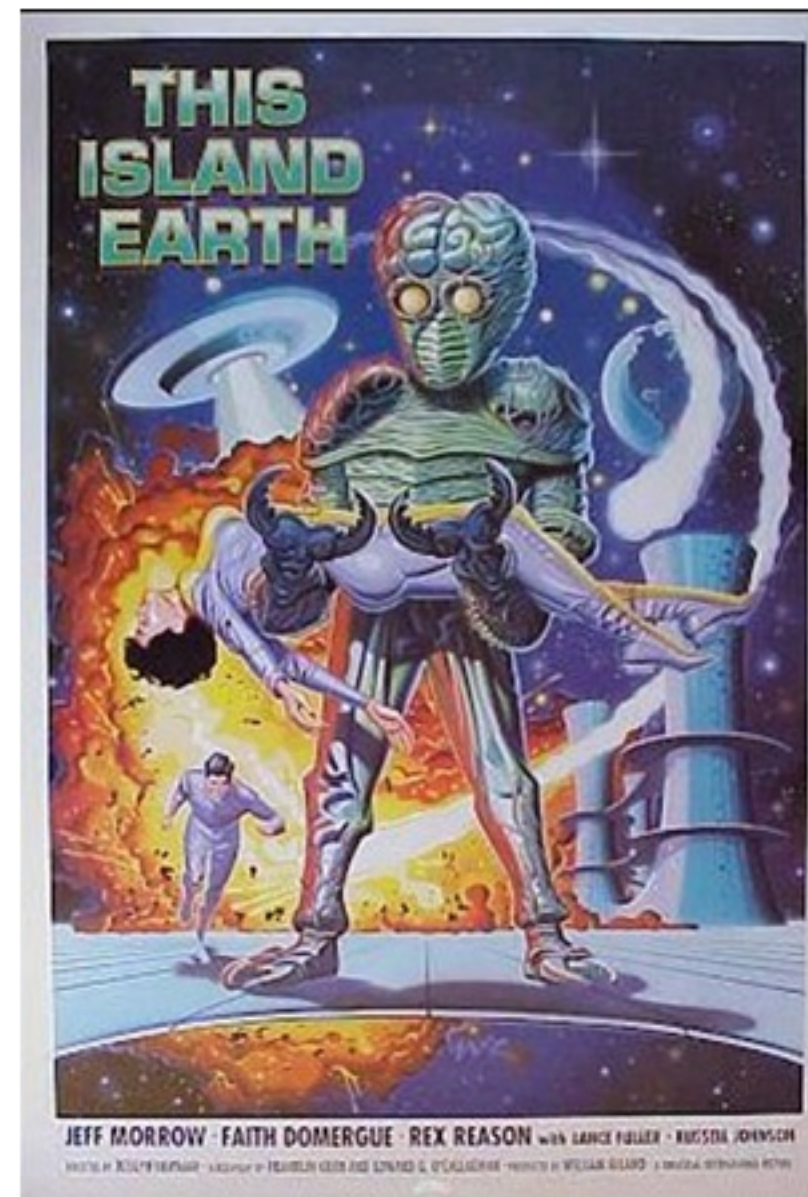
- Objectives
 - Define the concept of a ground string.
 - Define the term mutation operator.
 - Define the term mutant as it refers to a mutation operator.
 - Define mutation score as it is relative to mutation testing.
 - Explain the concept of a dead mutation.
 - Explain the concept of a stillborn mutant.
 - Draw a flowchart showing the process used to perform mutation testing.
 - List examples of program-level mutation operators.

- Original Program P
- Mutant P' of P
 - A program similar to P
 - P' differs from P by a single mutation
 - Each kind of mutation corresponds to a typical error programmers usually make

one thing that is different

A Mutant



- “Off--by--one”, spelling, typos, etc..



Definition

- Ground string
– A string that is in a grammar *Every program has a grammar*
- Mutation Operator *grammar*
– A rule that specifies syntactic variations of strings generated from a grammar
- Mutant *→ one flaw*
– The result of one application of a mutation operator
- Mutation coverage
– For each mutant $m \in M$, TR contains exactly one requirement, to kill m .

Mutation testing

- Mutation testing introduces faults into software by creating many different versions of the program
 - Each version has one very small change (which introduces a fault) compared to the actual implementation.
-  Goal 
 - See if the test cases can detect the new fault

Mutation Operators

- Rules applied to a program to create mutants
 - Example: replace each operator with another operator $+ \Rightarrow -, *, /, \%$
 - Replace each logical operator with another logical operator
 - Replace each comparison operator with another equivalent operator

$\rightarrow == \quad !=, >=, <=, <, >$



Example

```
Boolean isGreaterThanSum(int a, int b, int c)
{ Boolean retVal = false;
  If (a > (b + c))
  {
    retVal = true;
  }
  Return retVal;
}
```

true

false

*- , / , * , %*

> = , = = , < , < = , ! =

A B C

5 2 2

4 2 2

3 2 2



Java Mutation Operators

$if(x > y) \Rightarrow if(x > y + 1)$

Operator	Description
AOR	Arithmetic Operator Replacement ✓
AOI	Arithmetic Operator Insertion ✓
AOD	Arithmetic Operator Deletion ✓
ROR	Relational Operator Replacement
COR	Conditional Operator Replacement
COI	Conditional Operator Insertion
COD	Conditional Operator Deletion
SOR	Shift Operator Replacement
LOR	Logical Operator Replacement
LOI	Logical Operator Insertion
LOD	Logical Operator Deletion
ASR	Assignment Operator Replacement

$if(y > 0)$
 $z[y - 1] = x;$

$<<, >>$

1 Arithmetic Operators

The Java programming language supports five arithmetic operators for all floating-point and integer numbers; (1) +, (2) -, (3) *, (4) /, and (5) %. These operators are all binary. However, both + and - have unary versions. Four short-cut arithmetic operators are defined; (1) op++, (2) ++op, (3) op--, and (4) --op.

- **AOR_B** : Arithmetic Operator Replacement
Replace basic binary arithmetic operators with other binary arithmetic operators.
- **AOR_U** : Arithmetic Operator Replacement
Replace basic unary arithmetic operators with other unary arithmetic operators.
- **AOR_S** : Arithmetic Operator Replacement
Replace short-cut arithmetic operators with other unary arithmetic operators.
- **AOI_U** : Arithmetic Operator Insertion
Insert basic unary arithmetic operators.
- **AOI_S** : Arithmetic Operator Insertion
Insert short-cut arithmetic operators.
- **AOD_U** : Arithmetic Operator Deletion
Delete basic unary arithmetic operators.
- **AOD_S** : Arithmetic Operator Deletion
Delete short-cut arithmetic operators.

2 Relational Operators

What can happen to a mutant?

• Stillborn Mutant \Rightarrow A mutant \Rightarrow if (x > 0)
which will not compile.

• Killed Mutant A mutant which is discovered
by executing a unit test.

• Live Mutant \rightarrow A mutant which
is not detected by the test suit.

• Stubborn Mutant

Mutants which
result in equivalent
execution.

A mutant which results in
intention but not proposition.



How does this impact out

test cases

```
public int sum (int a, int b)
{
    return a+b;
}
```

	7	2	4
a-b ✓	3	3	6
<u>a*b</u> ✓	0	0	0
a/b ✓			
a'.b ✓	-2	-2	-4
.	.	.	.

Equivalent Mutant

```
int index=0;
while (...)
{
    ...;
    index++;
    if (index==10)
        break;
}
```

*if (index >= 10)
break;*

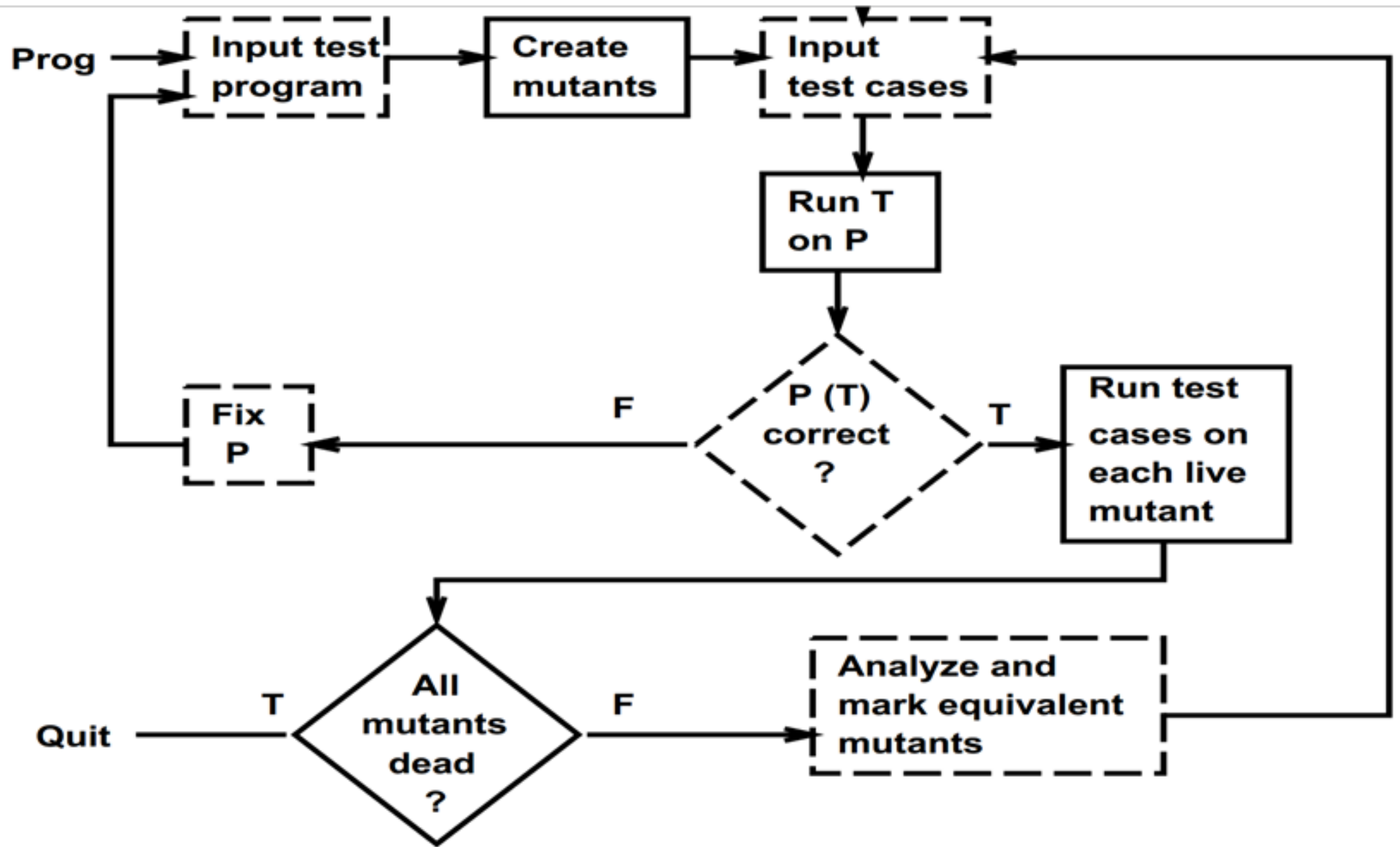
Stubborn Mutant

```
int sumNumbers(int x, int y)
{
  int sum = 0;
  int index;
  if (y > x)  $\Rightarrow$  if (y >= x)
  {
    for (index = x; index < y; index++)
    {
      sum += index;
    }
  }
  return sum;
}
```

Mutation Score

$$MS = \frac{\# \text{ of Killed Mutants}}{\# \text{ of Mutants}}$$

Mutation testing Complexity



Premise of mutation testing

- In practice, if the software contains a fault, there will usually be a set of mutants that can only be killed by a test case that also detects that fault.

Limitations and Problems

- **Difficult to identify equivalent mutants**
 - Same behavior as the original program
 - They can not be killed
 - Important but very difficult to identify them
- **Difficult to kill stubborn non--equivalent mutants**
 - May be non--equivalent but still very difficult to kill
- **Computational Cost of Mutation Testing**
 - Big number of mutation operators that create a vast number of mutants
(not always relevant ones)
 - Typically there is a large number of mutants for even small software units
 - Computationally expensive to test all these mutants against all the test cases
 - Mutation analysis requires large amounts of computation
- **Manual Labor when using Mutation Testing**
 - Manual equivalent mutant detection is quite tedious
 - Developing mutation adequate test cases can be very labor--intensive



Mutation Tools