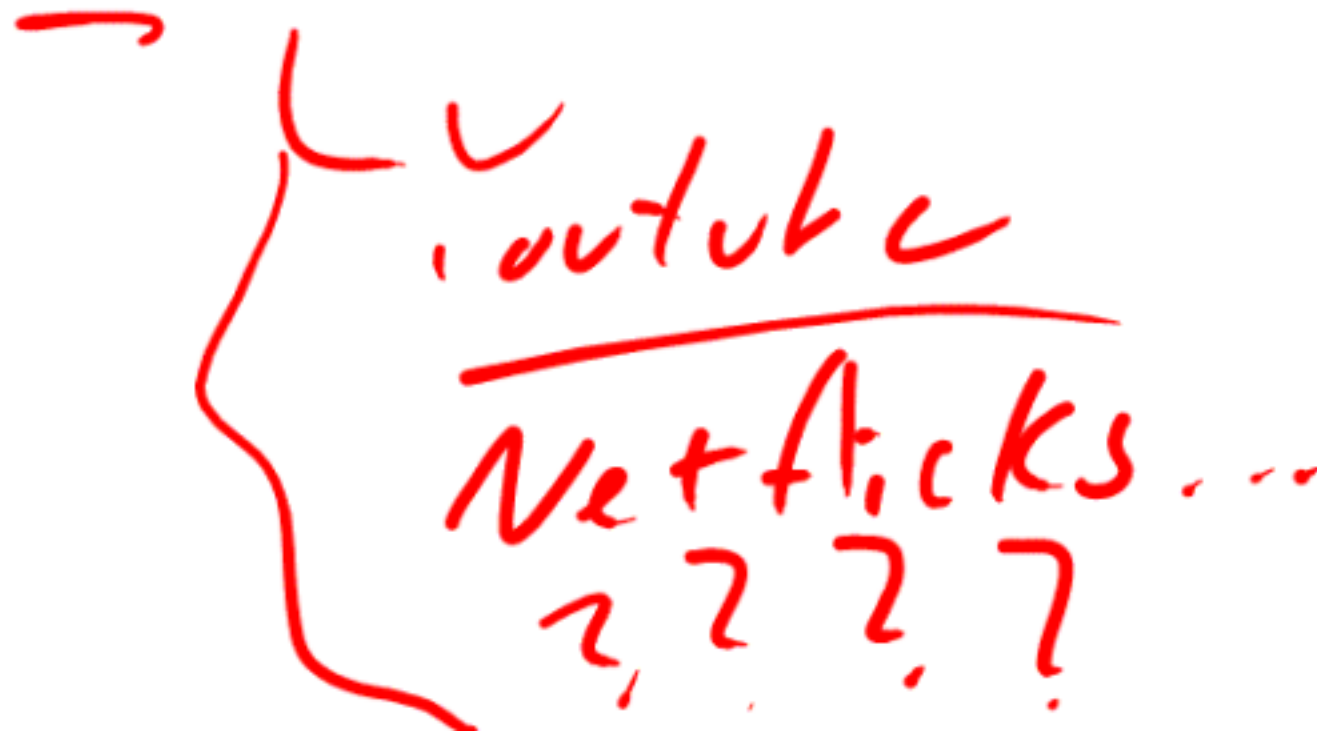




# SE3910 – REAL TIME SYSTEMS

Audio and Video Constraints



# ROADMAP

- Today
  - An Introduction to audio *video*
- Friday (Tentative)
  - Real Time Coding Standards -

# OBJECTIVES

- Explain the relationship between bandwidth and image quality for a video stream.
- Calculate the bandwidth needed to deliver a given quality image
- Explain the stroboscopic effect
- Calculate the maximum data rate of a channel under both noiseless and noisy signal conditions
- Explain the Nyquist theorem related to sampling
- Calculate the minimum sampling rate necessary to transmit a signal using the Nyquist Theorem
- Explain the relationship between the number of bits and quality when sampling a signal

• How is an image stored in memory?

100



⇒ Depends on file

"Bit mapped format"

Each pixel is in memory

2D Array of pixels

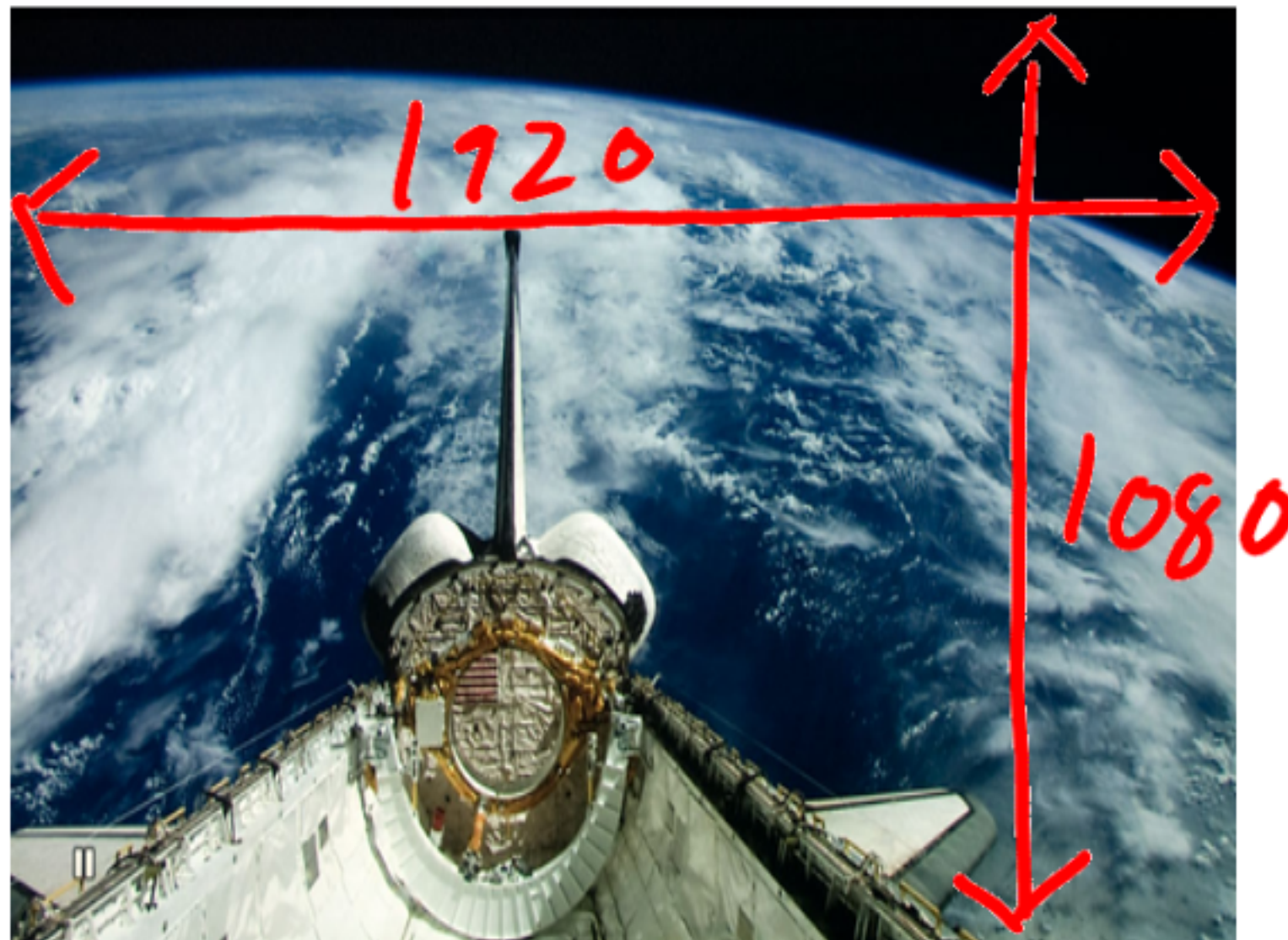
Grayscale ⇒ Each pixel has 1 byte



100 x 100 ⇒ 10000 pixels  
≈ 10 KB

WHAT DOES 1080P MEAN?

- **1080p**: The modern Television Standard



60 frames per second

are transmitted.

# HOW BIG IS A 1080P IMAGE?

- Calculation: Width x Height X bytes per pixel

$$\begin{array}{r} 1920 \times 1080 \times 24 \text{ bits per pixel} \\ \times 3 \\ \hline 6220800 \text{ bytes/image} \\ 6220 \text{ KB} \\ 6.22 \text{ MB} \end{array}$$

SECOND?  
(UNCOMPRESSED)

- Bandwidth = Size of one frame x frame size ~~rate~~

$$6.22 \text{ MB} \times 60 \frac{\text{frames}}{\text{second}}$$

$$\Rightarrow \text{Bandwidth} \quad \begin{array}{r} 6.22 \\ \times 60 \\ \hline \end{array}$$

$$373.20 \text{ MB/second}$$

- Depends on how much motion we have in the picture...

HOW FAST DO WE NEED AN IMAGE TO SHOW?

Downhill skiing



FAST

Fast frame rate

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Curling



Slow

Slow frame rate

This image

Steamboat Willie 12 fps

Movie Theater

24 fps

60-100 fps



# THE STROBOSCOPIC EFFECT

- Have you ever noticed something that is in motion seem to stop?

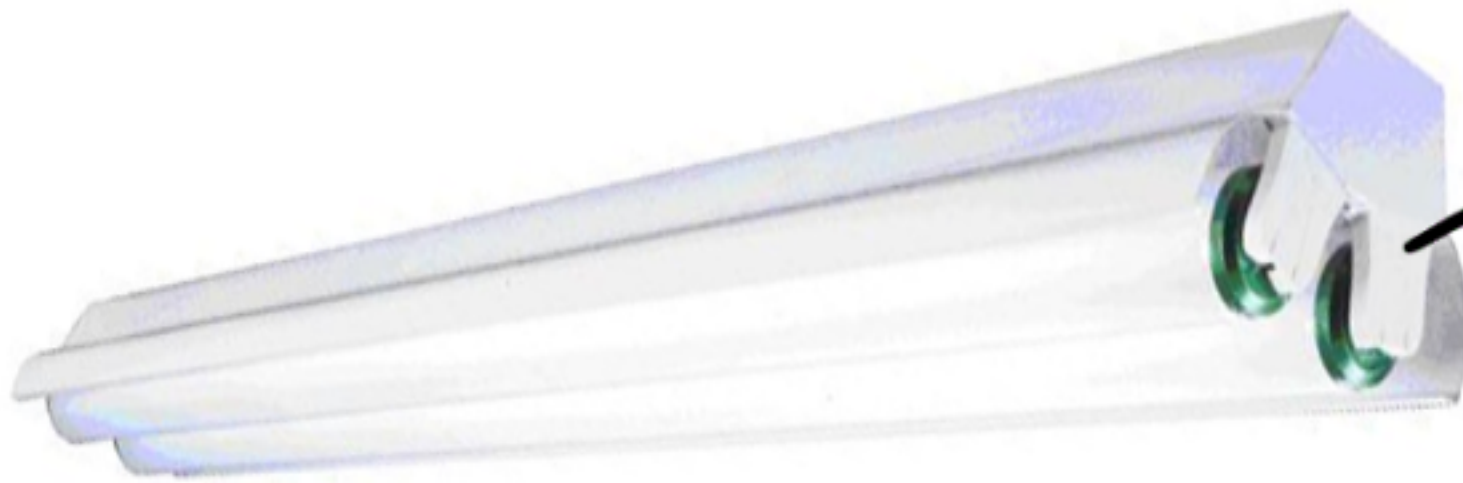
Car wheel

Water drop ...

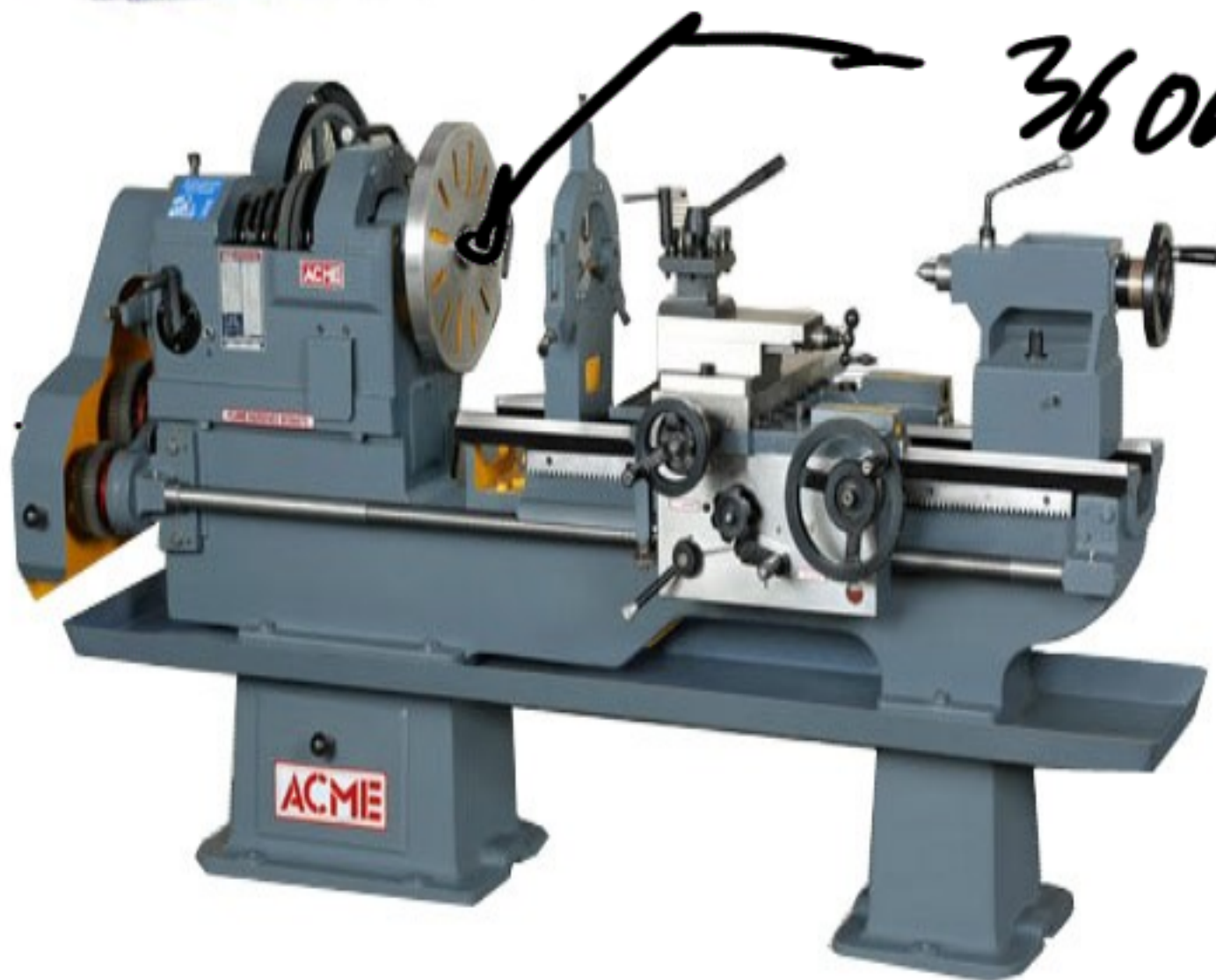
# SOME EXAMPLE VIDEOS SHOWING STROBOSCOPIC EFFECT

- [http://upload.wikimedia.org/wikipedia/commons/thumb/7/77/Propeller\\_strobe.ogv/220px--Propeller\\_strobe.ogv.jpg](http://upload.wikimedia.org/wikipedia/commons/thumb/7/77/Propeller_strobe.ogv/220px--Propeller_strobe.ogv.jpg)
- [http://upload.wikimedia.org/wikipedia/commons/thumb/e/ef/The\\_wagon-wheel\\_effect.ogv/220px--The\\_wagon-wheel\\_effect.ogv.jpg](http://upload.wikimedia.org/wikipedia/commons/thumb/e/ef/The_wagon-wheel_effect.ogv/220px--The_wagon-wheel_effect.ogv.jpg)

A SAFETY MOMENT



120 times  
second








3600 RPM...

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This is an image

# TRANSMITTING DATA

- Physical Layer 
  - You didn't talk too much about this in Network Protocols
  - Can occur through many mediums
    - Twisted Pair 
    - Coaxial Cable 
    - Fiber Optics 
    - Wireless 

# WHAT IS THE MAXIMUM RATE OF A CHANNEL?



- Henry Nyquist (AT&T Engineer (1924) and Claude Shannon (1948)
- Nyquist Theorem
- maximum data rate =  $2H \log_2 V \frac{\text{bits}}{\text{sec}}$

$$2 \cdot H \cdot \log_2 2 \text{ bit/s}$$

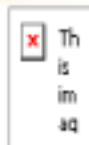
$$2 \cdot H \cdot 1$$

$\rightarrow 30 \text{ kHz}$

Bandwidth of medium

# of levels

0, 1



Theoretical Limit

# WHAT IS THE MAXIMUM RATE OF A CHANNEL WITH NOISE?



3kHz

Bandwidth (Hz)	SN (db)	Maximum Number of Bits per second
3000	0	3000
3000	10	10378.29486
3000	20	19974.63445
3000	30	29901.67878
3000	40	39863.56993
3000	50	49828.9647
3000	60	59794.71004
3000	70	69760.49043
3000	80	79726.27432

- Claude Shannon (1948)

- maximum number of  $\frac{\text{bits}}{\text{second}} = H \log_2 \left( 1 + \frac{S}{N} \right)$

Note: S/N Usually given in DB. To use, must convert using formula  $10^{DB/10}$

Handwritten calculation:

$$3000 \cdot \log_2 \left( 1 + 10^{30/10} \right)$$

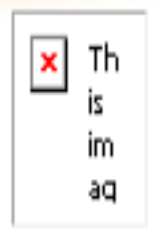
$$= 3000 \cdot \log_2 (1 + 1000)$$

more bandwidth

decibel

DB/10

# MAXIMUM BANDWIDTH OF CHANNEL UNDER NOISE

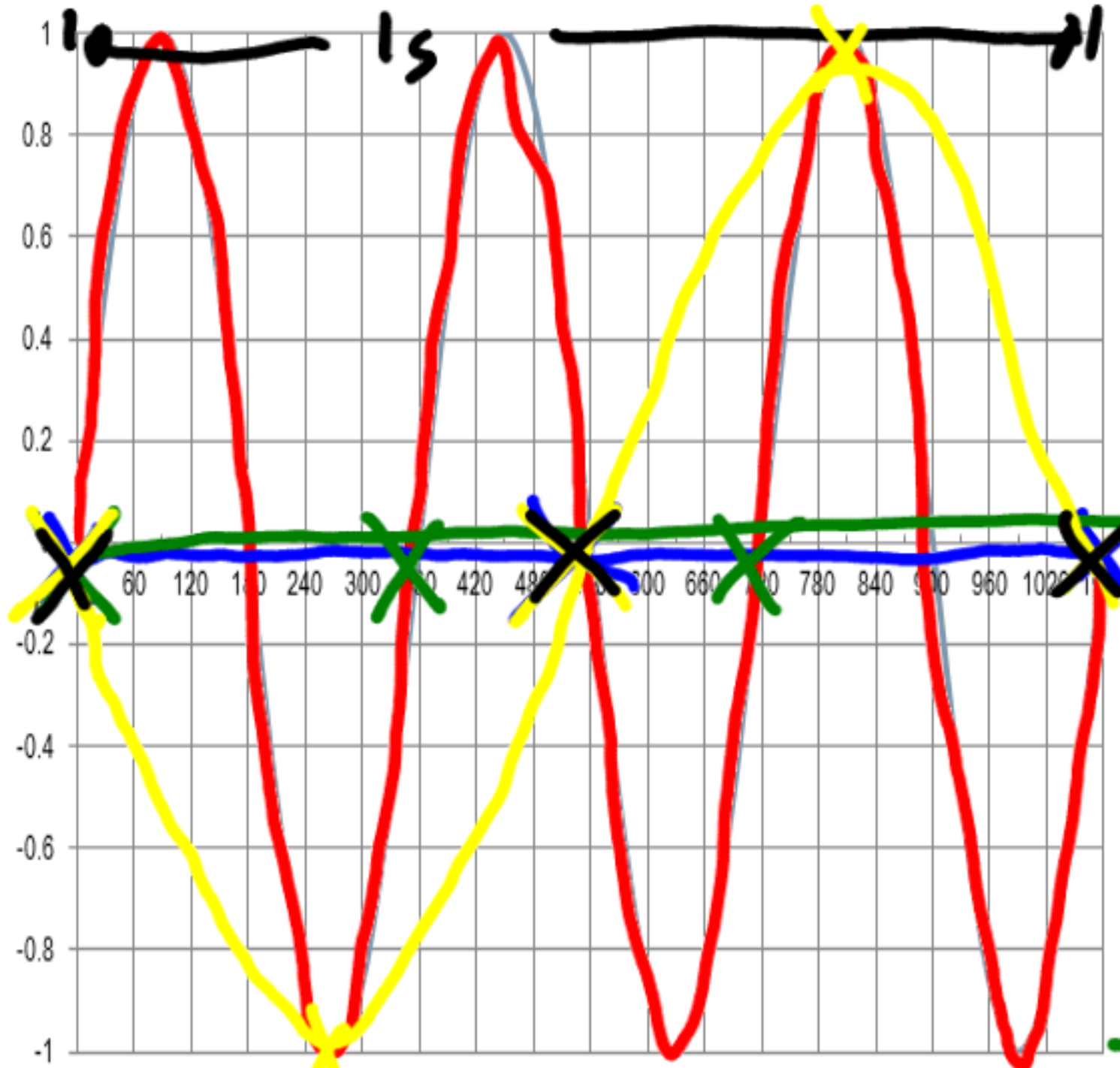


WIRING TYPES

Wiring Type	Bandwidth	
CAT 3 — "Phone Line"	16MHz	
CAT 5 "ethernet cables"	100 MHz	
Coaxial Cable (50 Ohm) ↳ "cable modem"	<u>1-2 GHz</u>	
Fiber Optic	50000 GHz	



# SAMPLING THEOREM




What is my frequency?  
3 Hz

2x per second

3x per second

4x/5

6x/2

 This is imaq



# SAMPLING THEOREM

- Nyquist Criterion
- $\Rightarrow \underline{f_s} > \underline{2B}$

3k BW  $\Rightarrow$  6k/s

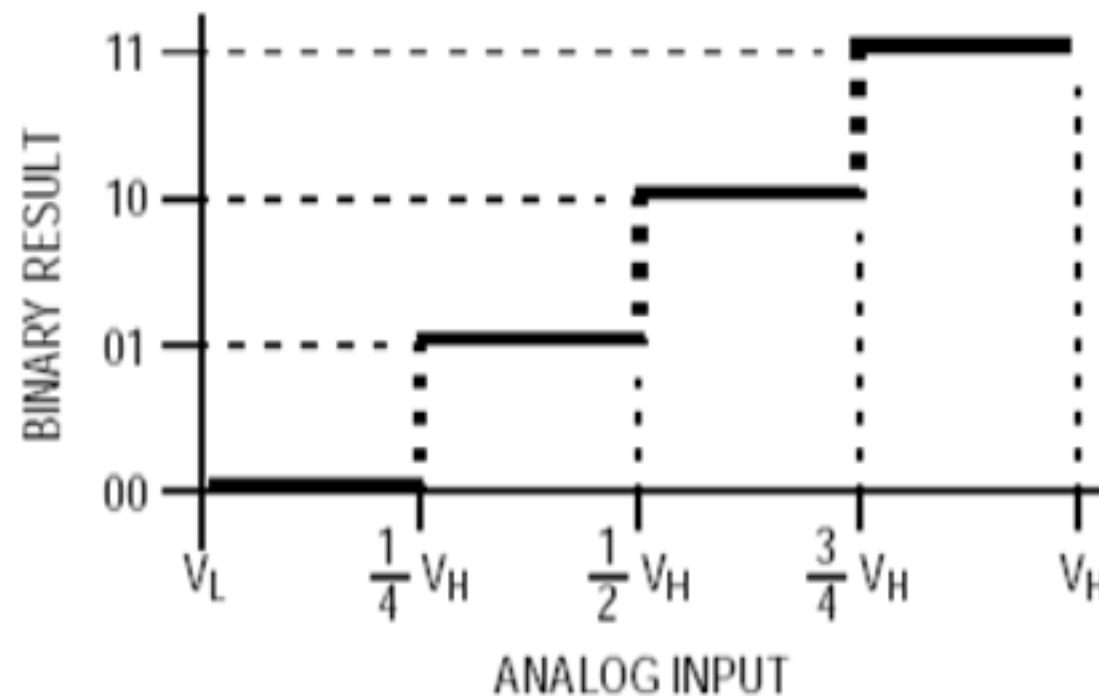
- Nyquist Rate  $\Rightarrow 2B$
- Audio Sampling:

Sample rate	Quality level	Frequency range
11,025 Hz	Poor AM radio (low-end multimedia)	0-5,512 Hz
22,050 Hz	Near FM radio (high-end multimedia)	0-11,025 Hz
32,000 Hz	Better than FM radio (standard broadcast rate)	0-16,000 Hz
44,100 Hz	CD	0-22,050 Hz
48,000 Hz	Standard DVD	0-24,000 Hz
96,000 Hz	High-end DVD	0-48,000 Hz

Telephone 8kHz Telephone 0-3.2kHz

# DISCRETIZATION?

- Consider an analog signal that will vary between two values – say 0 and  $V_H$  volts
- Discretization refers to the “levels” the ADC is able to resolve the analog signal to:
  - a 2-bit converter can resolve 4 different discrete levels

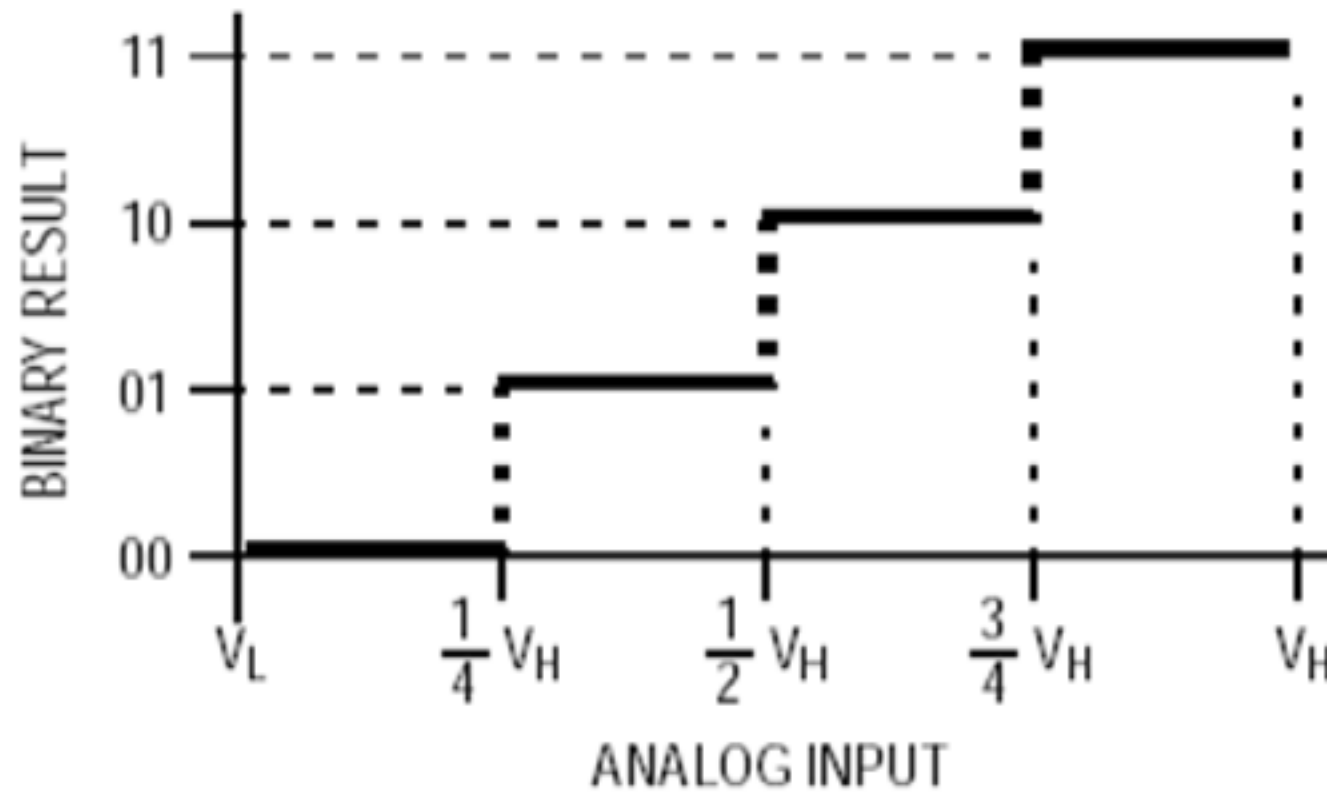


A/D CON

19

✘ This is incorrect

# QUANTIZATION ERROR



Difference between the actual analog value and quantized digital value due is called **quantization error**.

- Due either to rounding or truncation.

# NOISE AND THE NUMBER OF BITS

$$\text{SQNR} = 20 \log_{10}(2^Q) \approx 6.02 \cdot Q \text{ dB}$$